

Fiber-Optic Airplane Seismology on the Northeast Greenland Ice Stream

Andreas Fichtner^{*1}, Coen Hofstede², Brian L. N. Kennett³, Niels F. Nymand⁴, Mikkel L. Lauritzen⁴, Dimitri Zigone⁵, and Olaf Eisen^{2,5,6}

Abstract

We present distributed fiber-optic sensing data from an airplane landing near the EastGRIP ice core drilling site on the Northeast Greenland Ice Stream. The recordings of exceptional clarity contain at least 15 easily visible wave propagation modes corresponding to various Rayleigh, pseudoacoustic, and leaky waves. In the frequency range from 8 to 55 Hz, seven of the modes can be identified unambiguously. Based on an a priori firn and ice model that matches *P*-wave dispersion and the fundamental Rayleigh mode, a Backus–Gilbert inversion yields an *S*-wavespeed model with resolution lengths as low as a few meters and uncertainties in the range of only 10 m/s. An empirical scaling from *S* wavespeed to density leads to a depth estimate of the firn–ice transition between 65 and 71 m, in agreement with direct firn core measurements. This work underlines the potential of distributed fiber-optic sensing combined with strong unconventional seismic sources in studies of firn and ice properties, which are critical ingredients of ice core climatology, as well as ice sheet dynamics and mass balance calculations.

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Introduction

Firn is the transition material between snow and ice formed by a sequence of processes, including the settling and rounding of crystals, recrystallization, and viscoplastic deformation (Gow, 1968). Although firn often accounts for only a small fraction of ice sheet mass and volume, detailed knowledge of its properties is essential for ice sheet mass balance calculations (e.g., Helsen *et al.*, 2008), ice core climatology (e.g., Parrenin *et al.*, 2012), estimates of surface melt (e.g., van den Broeke, 2005), and the correction of seismic reflection data for near-surface effects (e.g., Schlegel *et al.*, 2019).

For several decades, firn properties have been estimated noninvasively using seismic refraction data (Thiel and Ostenso, 1961; Kohnen and Bentley, 1973; Schlegel *et al.*, 2019; Hollmann *et al.*, 2021) and horizontal-to-vertical spectral ratios (Lévêque *et al.*, 2010), sometimes combined with empirical conversions from seismic wavespeeds to density (Kohnen, 1972; Diez *et al.*, 2014). Alternatively, the distribution of *S* wavespeed may be estimated from seismic noise interferometry (Zhou *et al.*, 2023).

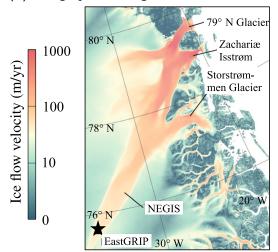
New opportunities for seismic studies of firn come from multiple directions. Distributed acoustic sensing (DAS) combines unprecedented spatial coverage with a large bandwidth (Lindsey et al., 2020; Lindsey and Martin, 2021; Paitz et al., 2021), and has proven to be logistically feasible and beneficial in glacial environments (Walter et al., 2020; Hudson et al., 2021; Klaasen et al., 2021, 2022; Fichtner et al., 2022). Also recently, unconventional seismic sources related to human activity have been recognized more widely as valuable carriers

1. Department of Earth Sciences, ETH Zurich, Zurich, Switzerland, https://orcid.org/0000-0003-3090-963X (AF); 2. Alfred Wegener Institute, Helmholtz Centre for Polar and Marine Research, Bremerhaven, Germany, https://orcid.org/0000-0002-6015-6918 (CH); https://orcid.org/0000-0002-6380-962X (OE); 3. Research School of Earth Sciences, The Australian National University, Canberra, Australia, https://orcid.org/0000-0003-2206-5350 (BLNK); 4. Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark, https://orcid.org/0000-0003-1868-7771 (NFN); https://orcid.org/0000-0002-5951-9339 (MLL); 5. Université de Strasbourg/CNRS, Institut Terre et Environnement de Strasbourg, Strasbourg Cedex, France, https://orcid.org/0000-0003-2383-8271 (DZ); 6. Department of Geosciences, University of Bremen, Bremen, Germany

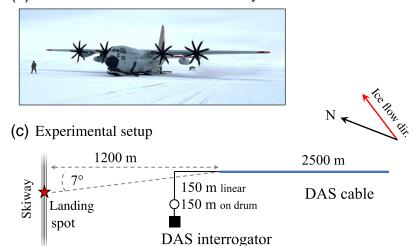
^{*}Corresponding author: andreas.fichtner@erdw.ethz.ch

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(a) Geographic setting



(b) C-130 Hercules on EastGRIP skiway



of information on subsurface structure (Dou et al., 2017; Sager et al., 2022).

In this work, we harness DAS data from an airplane landing near the EastGRIP ice core drilling site located in the upstream part of the Northeast Greenland Ice Stream (NEGIS; Fig. 1a). With a length of nearly 600 km, NEGIS accounts for \sim 12% of Greenland's total ice discharge (Rignot and Mouginot, 2012), thereby attaching special relevance to detailed firn models. The strength and duration of the airplane source produced seismic data of remarkable clarity, containing 15 visually discernable wave propagation modes, many of which can be identified and used to constrain S wavespeed with meter-scale resolution and uncertainties of few meters per second depending on depth.

Experimental Setup and Phenomenology

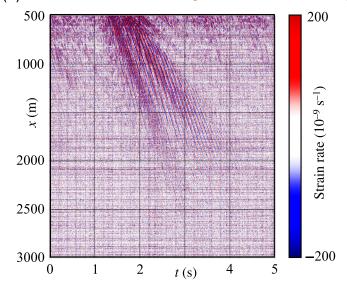
Realizing that an airplane landing may be the strongest available seismic source, we deployed 3000 m of Solifos BRUfield fiber-optic cable (light-weight tactical, nonmetallic loose-tube) for DAS recording. To maximize sensitivity to waves excited near the expected landing spot, the cable runs perpendicular to the skiway, except for the first few hundred meters as shown in Figure 1. One of four single-mode fibers was connected to a Silixa iDAS with 10 m gauge length, and interrogated with 1 kHz sampling frequency and 2 m channel spacing. To ensure good coupling, a snowcat produced a trench for the cable, which was then covered by snow. We estimate the average burial depth of the cable at >50 cm. For our analyses, we use the last 2500 m of the cable, which are nearly linear,

Figure 1. Summary of the experimental setup. (a) Flow velocity of Northeast Greenland Ice Stream (NEGIS; Joughin *et al.*, 2018) with its outlet glaciers and the location of the EastGRIP camp. (b) Photograph of the C-130 Hercules on the skiway, shortly after the landing that produced the data in Figure 2. (c) Geometry of the 3000 m distributed acoustic sensing (DAS) cable relative to the skiway and the landing spot. We analyze data from the last 2700 m of the cable, which are nearly linear and orthogonal to the skiway. The black arrow indicates true north (N), and the red arrow indicates the direction of ice flow at the surface.

orthogonal to the skiway and at sufficient distance from the EastGRIP camp to avoid the presence of significant anthropogenic noise, mostly originating from the generator.

The C-130 Hercules touched down on a groomed skiway at UTC 17:02:06 on 26 July 2022 at a position that makes an angle between ~3° and 7° to the linear cable segment. Its weight and sinking speed are estimated around 60 t and 1 m/s, respectively. A record section of the raw strain rate recordings is displayed in Figure 2a. Although individual components of the wavefield are difficult to discern in the time-space domain, a transformation to the frequency-phase velocity domain via a simple 2D Fourier transform shown in Figure 2b reveals ~15 visually distinguishable wave propagation modes. These include several Rayleigh wave modes with cutoff velocity around 1900 m/s, a leaky mode propagating faster than ~1900 m/s, as well as pseudoacoustic modes that correspond to P waves trapped in the firn layer, which acts as a waveguide. Thanks to the exceptional clarity of the data, no additional preprocessing of the raw data was needed.

(a) Time domain DAS recording



The modes were identified through direct synthesis of the frequency-phase speed spectrum for a surface source (Kennett, 2023) that we employed for the construction of an initial model, described in more detail subsequently. This approach

allows mapping of modal extension into the leaking mode

Phase Velocity Inversion

regime and so includes the P mode behavior.

The unusual bandwidth combined with the large number of identifiable modes carries detailed information about the seismic properties of the upper few hundred meters of the ice sheet and the firn layer in particular. Radar soundings constrains the topographic variations of these layers to be on the order of only few meters over several kilometers distance (e.g., Franke *et al.*, 2022), which enables the use of modeling and inversion techniques for stratified media without significant approximation errors. To account for the nonzero incidence angle of \sim 5° on average, we multiply all apparent phase velocities with $\cos(5^\circ) \approx 0.996$.

To avoid biases introduced by subjective discretization and regularization, we implement a Backus–Gilbert inversion of the dispersion data (Backus and Gilbert, 1968, 1970; Fichtner, 2021). This comes with the additional benefit of automatically providing objective model errors and resolution (averaging) lengths. A prerequisite for Backus–Gilbert inversion is the availability of an initial model that explains the main features of the data and thereby permits a reasonable linearization. In the following paragraphs, we first describe the initial

(b) Frequency–phase velocity domain DAS recording

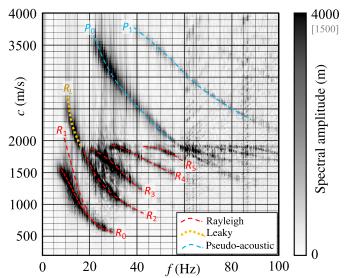


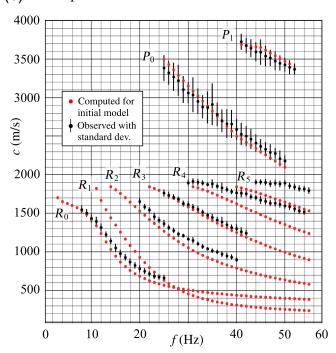
Figure 2. Raw data summary. (a) Time-domain DAS recording along the straight section of the cable between 500 and 3000 m. Time t=0 corresponds to UTC 17:02:08 on 26 July 2022. (b) Frequency–phase velocity representation of the raw data. The most prominent features, marked with dashed curves, include several Rayleigh wave modes (R_i) , a leaky mode (R_L) , and pseudoacoustic modes (P_i) . The first Rayleigh overtone R_1 is only weakly excited and close to the strong fundamental mode R_0 . Frequencies from 60 to 100 Hz are shown with a lower color scale saturation of 1500 m in spectral amplitude to improve the visibility of higher Rayleigh wave modes.

model construction before presenting the results of the Backus-Gilbert inversion.

Initial model

The initial model, displayed in Figure 3a, is the result of a trial-and-error procedure primarily aiming to explain the fundamental-mode Rayleigh wave, and the P-wave modes P_0 and P_1 to within the observational standard deviations, estimated as the half-width of the phase velocity–frequency peaks in Figure 2b. For this, we took advantage of the long-established prior knowledge that the depth dependence of seismic velocities in firn approximately follows an exponential (Brockamp and Pistor, 1967; Kohnen and Bentley, 1973). Using constant instead of exponential velocities just within the top 1 m significantly improves the fit to the fundamental Rayleigh mode. This feature plausibly reflects the more rapid compaction of snow around the EastGRIP camp in response to human activity. The





initial density model is scaled to the initial v_p model following the relation proposed by Kohnen (1972).

10

z(m)

100

300

Figure 3b illustrates that the initial model, by design, reproduces the fundamental Rayleigh mode and the P-wave mode dispersion measurements. This match enables the identification of the other modes, including the realization that R_1 is only weakly excited. Discrepancies between observed and modeled phase velocities remain for the higher Rayleigh modes, especially for the fourth and fifth overtones. These are the sources of information about more structural details in the ν_s model that we consider in the section on Backus–Gilbert inversion.

Backus-Gilbert inversion

0.5

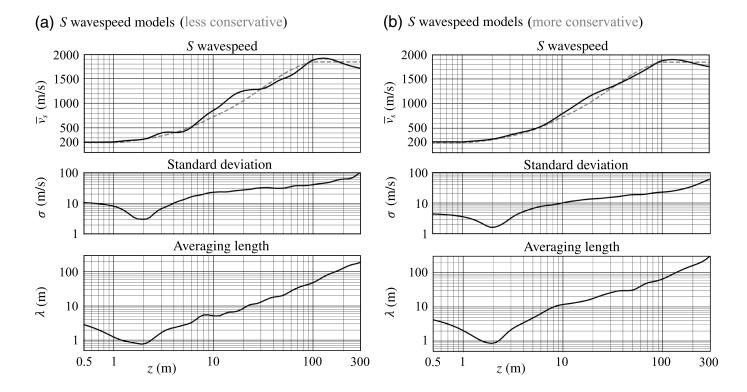
The initial model serves in the calculation of sensitivity kernels G_i , which play a double role in Backus–Gilbert theory. They link the difference $\delta c_i = c_i^{\text{obs}} - c_i$ between observed and calculated phase velocities for the ith measurement to the v_s distribution via $\delta c_i = \int G_i(z') \delta v_s(z') dz'$. In addition, they are basis functions of averaging kernels, $A(z',z) = \sum_i a_i(z) G_i(z')$ that produce a depth-averaged version of the S wavespeed, $\overline{v}_s(z) = \int A(z',z) v_s(z') dz'$. Though $v_s(z')$ is not directly observable, the average can be computed directly and uniquely from the data as $\overline{v}_s(z) = \sum_i a_i(z) \delta c_i$. Basis coefficients $a_i(z)$ that produce averaging kernels with optimal concentration

Figure 3. Initial model for phase velocity inversion. (a) Initial depth distributions of P wavespeed (v_p), S wavespeed (v_s), and density (ρ). Functional forms in the intervals 0–1 m, 1–11 m, 11–100 m, and >100 m are indicated for seismic velocities. (b) Phase velocity dispersion calculated for the initial model. Observations with error standard deviations are shown in black and calculated values in red.

around a target depth z can be found by maximizing the deltaness $\lambda(z)=12\int(z-z^{'})^2A^2(z^{'})dz^{'}$, which simultaneously provides a conservative estimate of the averaging or resolution length. Standard deviations of the averages, $\sigma(z)$, can be computed from the standard deviations of the observations, $\sigma^{\rm obs}$ via $\sigma^2(z)=\sum_i [a_i(z)\sigma_i^{\rm obs}]^2$.

For the inversion we employ all available pairs of observed and calculated phase velocities with 1 Hz frequency spacing shown in Figure 3b. Omitting the first overtone R_1 , because of its weak excitation and large observational errors results in 94 data points. In the construction of S-wavespeed models, the averaging length λ and the standard deviation σ are antagonistic. Increasing λ decreases σ and vice versa, thereby giving rise to infinitely many models with a different balance between accuracy and resolution.

Two of these models are displayed in Figure 4. In accord with the mostly positive phase velocity residuals δc_i , the less



conservative one in Figure 4a shows several high-velocity deviations from the initial model, especially around 3 and 20 m depth. These are less pronounced in the more conservative version in Figure 4b, which has a larger averaging length but lower standard deviations. Within the upper 10 m, both the models have a vertical resolution or averaging length of few meters, increasing to few tens of meters around 100 m depth. Standard deviations of the inferred $\overline{\nu}_s$ reach the minimum well below 10 m/s near the surface and approach 100 m/s at several hundred meters depth. Code to produce a suite of alternative models is available in the model website referenced in the Data and Resources section.

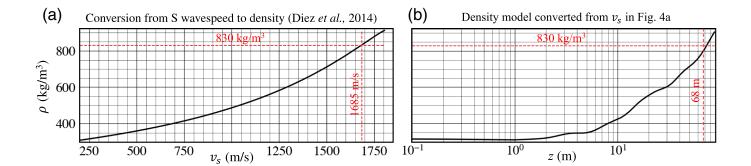
The averaging length scales of ~ 1 to few tens of meters within the upper 100 m can be considered conservative, because λ is a mathematically conservative measure that gives large weight to distant side lobes in the averaging kernels. In fact, ice core analyses show that firn and ice properties below several meters depth vary smoothly over seismic wavelength scales (Vallelonga *et al.*, 2014) and can be approximated by linear functions within the width of the averaging kernels. Though it is difficult to turn this into a quantitative argument, the smoothness suggests that the difference in depth in which $\overline{v}_s(z)$ and $v_s(z)$ reach a specific value is well below the averaging length.

Figure 4. Two of infinitely many averaged *S* wavespeed models with their associated standard deviation and averaging length. The less conservative model in panel (a) has shorter averaging lengths at the expense of larger standard deviations. The more conservative model in panel (b) has the opposite properties. The gray dashed line in the top panels marks the initial model.

Empirically Derived Density Profiles

Although dispersion curves and seismic travel times are primarily sensitive to wavespeeds, most glaciologically relevant information derives from density profiles. Empirical scaling relations have been estimated primarily from the comparison of seismic refraction profiles and direct density measurements on drill cores. Despite inherent limitations detailed in the Discussion section, the resulting density profiles carry useful approximate information, for instance, about the depth of the firn–ice transition at a density of 830 kg/m³.

We employ the empirical scaling derived from *SH*-wave diffraction by Diez *et al.* (2014). To make their relation applicable to our *SV*-wave model, we multiply *SH* wavespeeds by a factor of 0.95 that accounts for the typical 5% radial anisotropy in firn layers (e.g., Schlegel *et al.*, 2019). In the modified scaling, visualized in Figure 5a, a density of 830 kg/m³ corresponds to an *S* wavespeed of 1685 m/s. Using the model and uncertainties



from Figure 4a, the averaged S wavespeed \overline{v}_s exceeds $1685 \text{ m/s} \pm \sigma$ at depths between 65 and 71 m (Fig. 5b). This interval differs only at submeter scale when we choose other models with a different balance between accuracy and resolution, suggesting that the result is robust in this sense. Direct density measurements on firn cores at EastGRIP place the firn-density transition at \sim 65 m (Vallelonga *et al.*, 2014), in good agreement with our inference.

The scaling from wavespeed to density also translates the pronounced high-velocity anomaly near 20 m depth into a high-density anomaly. Although such an anomaly is not visible in the currently available firn core density measurements, the depth range around 20 m is characterized by anomalously thin annual layers (Vallelonga *et al.*, 2014). Because layer thickness affects the strength of induced radial anisotropy, this suggests that the seismically inferred high-density anomaly may be an artifact introduced by a scaling relation that is unaware of seismic anisotropy.

Discussion and Conclusions

Data quality and distributed fiber-optic sensing

Much of this work rests on the exceptional data quality, which has two major contributors in addition to low noise and the sheer strength of the source:

First, the strong velocity increase by a factor of ~ 10 over less than 100 m depth leads to wave trapping that is particularly effective. For comparison, P and S wavespeeds in the Earth's crust differ from those in the mantle only by a factor of ~ 2 (e.g., Kennett *et al.*, 1995). As a consequence, the character of the spectrum in Figure 2 resembles the displacement spectrum of the Sun (Kosovichev *et al.*, 1997), which has a similar wavespeed contrast as a firn layer (Christensen-Dalsgaard *et al.*, 1996). Furthermore, the lateral invariance of the medium produces clearly defined modes that hardly vary along the cable.

Figure 5. Scaling from wavespeed to density. (a) Scaling relation of (Diez *et al.*, 2014) modified to account for SV wavespeed that is typically \sim 5% lower than SH wavespeed within the firn layer. (b) Derived density profile.

Second, the availability of densely spaced DAS data is critical. With 2 m channel spacing, we achieve unaliased sampling of the wavefield, which has wavelength as low as ~ 15 m for the fundamental Rayleigh mode at 30 Hz. Because the cable is $\sim 10-100$ times longer than a wavelength, we obtain the resolution in wavenumber space that allows us to observe a large number of individual modes and measure their phase velocities with errors as low as a few meters per second. A direct consequence are the short averaging lengths and low uncertainties of the inferred S wavespeed profile.

Linearization and initial model

The success of the Backus-Gilbert inversion rests on the availability of a useful initial model, and in particular on the realization that the second strongly excited Rayleigh mode is R_2 and not R_1 . The latter derives from the prior knowledge that firn velocity profiles are approximately exponential. Ignoring this prior knowledge and trying to fit observed R_2 to calculated R_1 phase velocities with a global simulated annealing algorithm produced entirely implausible velocity models with a fast sequence of low-velocity layers and extreme P-wave anisotropy. That modes of lower order are less strongly excited than modes of a higher order is unusual but not impossible. It has previously been observed, for instance, in low-velocity sedimentary basins (Cruz-Atienza et al., 2016), and it can easily be explained mathematically by an approximate orthogonality of a modal eigenfunction and the forcing term (Gilbert, 1971).

We tested the effect of linearization by rerunning the inversion with some of the inversion results as new initial model.

However, such a one-step iterative improvement produced results that differed from the ones shown in Figure 4 by less than 1%, thereby suggesting that the problem is insignificantly nonlinear.

Limitations of wavespeed to density conversions

The empirical scaling from wavespeed to density inherits fundamental limitations from vastly different resolution lengths. Most scaling relations (e.g., Kohnen, 1972; Diez et al., 2014) link in situ or drill core measurements of density at centimeter scale to seismically inferred velocities with resolution lengths of many meters. As a consequence, each scaling depends on the seismic data used to derive it, and it may therefore not easily be transferred to other seismic experiments with different averaging kernels. This inconsistency is exacerbated by the presence of various types of anisotropy, which is neither represented in the scaling relations nor sufficiently resolvable with most seismic data. In summary, it does not seem unlikely that errors in the scaling relations dominate errors related to the insufficiency of the seismic data. Hence, small-scale details in the inferred density profiles, such as the high-density anomalies in Figure 5b, should be interpreted with caution.

Conclusions and further steps

We presented DAS data produced by an airplane landing near the EastGRIP ice core drilling site on the Northeast Greenland Ice Stream. The data are of exceptional clarity, especially in the frequency-phase velocity domain, in which around 15 wave propagation modes are easily visible. An inversion of seven identifiable modes produces an S-wavespeed profiles with resolution lengths as low as a few meters and standard deviations in the range of only 10 m/s. Empirically scaling to density provides an estimate of the firn-ice transition, which agrees with direct firn core measurements. Our experiment as a whole illustrates the potential of DAS combined with unconventional sources to provide detailed inferences of firn structure.

Yet, the work presented here is only a step towards a more comprehensive inversion. Possible improvements include (1) the incorporation of the leaky-mode observations, using, for instance, adjoint-based sensitivity kernels from numerical wave propagation, (2) the extension of the Backus–Gilbert method to multiple parameter classes, such as *P* wavespeed and density, which may make significant contributions at shallow depth, and (3) a fully nonlinear inversion for all relevant parameter classes using Monte Carlo sampling.

Data and Resources

All data as well as Python Jupyter notebooks to reproduce Rayleigh-wave dispersion and inversion are available on the Earth model website of the ETH Seismology and Wave Physics Group (https://www.swp.ethz.ch → Models). Code for the synthesis of the frequency-phase speed spectrum is available at Zenodo (doi: 10.5281/zenodo.7384357). A video with field work impressions can be found at https://www.youtube.com/watch?vCF7nZ7mxzSo. All websites were last accessed in May 2023.

Declaration of Competing Interests

The authors acknowledge that there are no conflicts of interest recorded.

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